

$$1. g(x) = \begin{cases} x + 5, & x < 2 \\ 11, & x = 2 \\ 2x - 1, & 2 < x < 5 \\ 20, & x = 5 \\ x + 4, & x > 5 \end{cases}$$

Find the following :

a) $\lim_{x \rightarrow -\infty} g(x) =$	b) $\lim_{x \rightarrow 2^-} g(x) =$	c) $\lim_{x \rightarrow 2^+} g(x) =$
d) $\lim_{x \rightarrow 2} g(x) =$	e) $\lim_{x \rightarrow 5^-} g(x) =$	f) $\lim_{x \rightarrow 5^+} g(x) =$
g) $\lim_{x \rightarrow 5} g(x) =$	h) $\lim_{x \rightarrow 6^+} g(x) =$	i) $\lim_{x \rightarrow \infty} g(x) =$

Use Continuity conditions to justify whether $f(x)$ is continuous or discontinuous . If discontinuous, identify type of discontinuity

$$2) f(x) = \begin{cases} x^2 + 5, & x \geq 3 \\ x^2 - 2, & x < 3 \end{cases}$$

3) Find the k value that will make the function $f(x)$ continuous.

$$b) f(x) = \begin{cases} \frac{x^2+x-6}{x+3}, & x \neq -3 \\ k, & x = 3 \end{cases}$$

PAST AP FREE-RESPONSE PROBLEMS COVERED BY THIS CHAPTER

Note: These and other questions can be found at
 apcentral.com.
 2003 AB 6a
 2006 BC 3c
 2008 AB 6d

MULTIPLE-CHOICE QUESTIONS

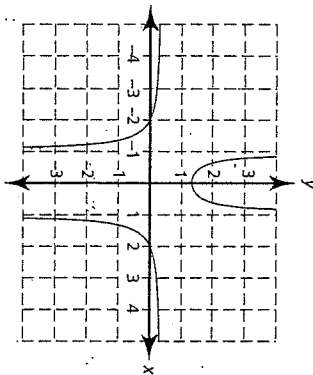
A calculator may not be used on the following questions.

- Evaluate the limit, if it exists: $\lim_{x \rightarrow 2} \frac{x^2 + x - 6}{2 - x}$.
 (A) 5
 (B) 3
 (C) -3
 (D) -5
 (E) The limit does not exist.
- Evaluate the limit, if it exists: $\lim_{x \rightarrow 9} \frac{\sqrt{x-5} - 2}{x-9}$.
 (A) $\frac{1}{4}$
 (B) $-\frac{1}{4}$
 (C) 1
 (D) 0
 (E) The limit does not exist.
- Evaluate the limit, if it exists: $\lim_{x \rightarrow 2} \frac{\frac{1}{x} - \frac{1}{2}}{x-2}$.
 (A) $\frac{1}{4}$
 (B) $-\frac{1}{4}$
 (C) 1
 (D) -1
 (E) The limit does not exist.

4)

For what value of k is the function $f(x) = \begin{cases} \frac{2x^2 + 5x - 3}{x^2 - 9}, & x \neq -3 \\ k, & x = -3 \end{cases}$ continuous at $x = -3$?

- (A) $-\frac{7}{6}$
 (B) $-\frac{5}{6}$
 (C) 0
 (D) $\frac{5}{6}$
 (E) $\frac{7}{6}$



5) The function $g(x)$ is shown in the graph above and is of the form $g(x) = \frac{x^2 + a}{bx^2 - 3}$. Which of the following could be the values of the constants a and b ?

- (A) $a = -2, b = -1$
 (B) $a = -2, b = -3$
 (C) $a = -4, b = 3$
 (D) $a = -4, b = -3$
 (E) $a = 4, b = 3$

6) Identify the vertical asymptotes for $f(x) = \frac{x^2 + 3x - 4}{x^2 + x - 2}$.

- (A) $x = -2, x = 1$
 (B) $x = -2$
 (C) $x = 1$
 (D) $y = -2, y = 1$
 (E) $y = -2$

$$1. g(x) = \begin{cases} x + 5, & x < 2 \\ 11, & x = 2 \\ 2x - 1, & 2 < x < 5 \\ 20, & x = 5 \\ x + 4, & x > 5 \end{cases}$$

Find the following :

<p>a) $\lim_{x \rightarrow -\infty} g(x) =$ $\lim_{x \rightarrow -\infty} x + 5 = \boxed{-\infty}$</p>	<p>b) $\lim_{x \rightarrow 2^-} g(x) =$ $\lim_{x \rightarrow 2^-} x + 5 = \boxed{7}$</p>	<p>c) $\lim_{x \rightarrow 2^+} g(x) =$ $\lim_{x \rightarrow 2^+} 2x - 1 = \boxed{3}$</p>
<p>d) $\lim_{x \rightarrow 2^-} g(x) \neq \lim_{x \rightarrow 2^+} g(x)$ $\lim_{x \rightarrow 2^-} g(x) = \boxed{DNE}$</p>	<p>e) $\lim_{x \rightarrow 5^-} g(x) =$ $\lim_{x \rightarrow 5^-} 2x - 1 = \boxed{9}$</p>	<p>f) $\lim_{x \rightarrow 5^+} g(x) =$ $\lim_{x \rightarrow 5^+} x + 4 = \boxed{9}$</p>
<p>g) $\lim_{x \rightarrow 5} g(x) =$ $\boxed{9}$</p>	<p>h) $\lim_{x \rightarrow 6^+} g(x) =$ $\lim_{x \rightarrow 6^+} x + 4 = \boxed{10}$</p>	<p>i) $\lim_{x \rightarrow \infty} g(x) =$ $\lim_{x \rightarrow \infty} x + 4 = \boxed{+\infty}$</p>

Use Continuity conditions to justify whether f(x) is continuous or discontinuous . If discontinuous, identify type of discontinuity

2) $f(x) = \begin{cases} x^2 + 5, & x \geq 3 \\ x^2 - 2, & x < 3 \end{cases}$

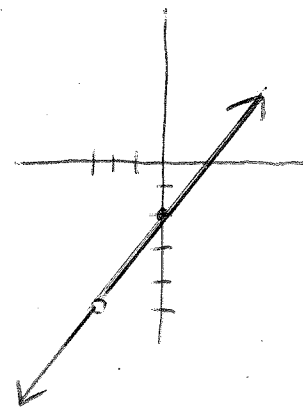
i) $f(3) = 3^2 + 5 = 14$
 ii) $\lim_{x \rightarrow 3^-} x^2 - 2 = 7$ $\lim_{x \rightarrow 3^+} x^2 + 5 = 14$ Since $\lim_{x \rightarrow 3^-} f(x) \neq \lim_{x \rightarrow 3^+} f(x)$
 $\lim_{x \rightarrow 3} f(x) = DNE$
 Nonremovable discontinuity
 since limit does not exist at $x=3$

3) Find the k value that will make the function f(x) continuous.

b) $f(x) = \begin{cases} \frac{x^2+x-6}{x+3}, & x \neq -3 \\ k, & x = -3 \end{cases}$

$$\lim_{x \rightarrow -3} \frac{x^2+x-6}{x+3} = \lim_{x \rightarrow -3} \frac{(x+3)(x-2)}{(x+3)} = -5$$

$k = -5$



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2003 AB 6a

2006 BC 3c

2008 AB 6d

MULTIPLE-CHOICE QUESTIONS

A calculator may not be used on the following questions.

1. Evaluate the limit, if it exists: $\lim_{x \rightarrow 2} \frac{x^2 + x - 6}{2 - x}$. $\lim_{x \rightarrow 2} \frac{(x+3)(x-2)}{-(x-2)} = -\frac{5}{1} = \boxed{-5}$
- (A) 5
(B) 3
(C) -3
(D) -5
(E) The limit does not exist.
2. Evaluate the limit, if it exists: $\lim_{x \rightarrow 9} \frac{\sqrt{x-5}-2}{x-9}$. $\frac{(\sqrt{x-5}+2)}{(\sqrt{x-5}+2)} = \lim_{x \rightarrow 9} \frac{x-5-4}{(x-9)(\sqrt{x-5}+2)}$
 $= \lim_{x \rightarrow 9} \frac{(x-9)}{(x-9)(\sqrt{x-5}+2)} = \frac{1}{\sqrt{4}+2} = \boxed{\frac{1}{4}}$
- (A) $\frac{1}{4}$
(B) $-\frac{1}{4}$
(C) 1
(D) 0
(E) The limit does not exist.
3. Evaluate the limit, if it exists: $\lim_{x \rightarrow 2} \frac{\frac{1}{x} - \frac{1}{2}}{x-2}$. $\frac{2-x}{2x} \cdot \frac{1}{x-2} = \lim_{x \rightarrow 2} \frac{-(x-2)}{2x(x-2)}$
 $\frac{1}{x-2} \cdot \frac{1}{x-2}$ $= \lim_{x \rightarrow 2} \frac{-(x-2)}{2x(x-2)} = \boxed{-\frac{1}{4}}$
- (A) $\frac{1}{4}$
(B) $-\frac{1}{4}$
(C) 1
(D) -1
(E) The limit does not exist.

4) For what value of k is the function $f(x) = \begin{cases} \frac{2x^2 + 5x - 3}{x^2 - 9}, & x \neq -3 \\ k, & x = -3 \end{cases}$

continuous at $x = -3$?

(A) $-\frac{7}{6}$

(B) $-\frac{5}{6}$

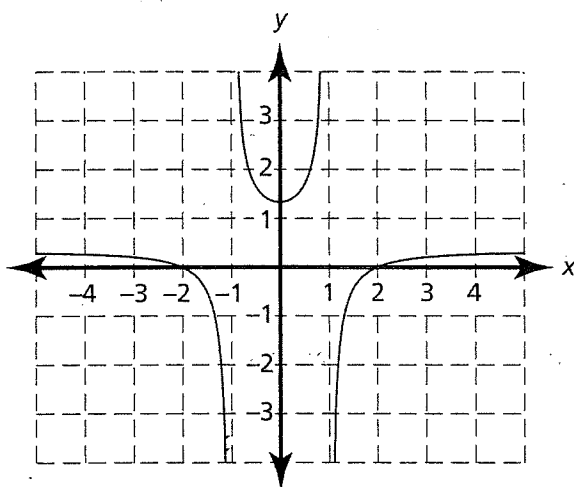
(C) 0

(D) $\frac{5}{6}$

(E) $\frac{7}{6}$

$$\lim_{x \rightarrow -3} \frac{(2x-1)(x+3)}{(x+3)(x-3)} = \frac{-6-1}{-3-3} = \frac{-7}{-6} = \frac{7}{6}$$

$k = 7/6$



x-int: $(-2, 0)$ $(2, 0)$

V.A: $x = -1, x = 1$

$x^2 + a = 0$ at $x = 2$

$2^2 + a = 0$ $a = -4$

$bx^2 - 3 = 0$: at $x = 1, x = -1$

$b(1)^2 - 3 = 0$ $b = 3$

5) The function $g(x)$ is shown in the graph above and is of the form

$g(x) = \frac{x^2 + a}{bx^2 - 3}$. Which of the following could be the values of the

constants a and b ?

(A) $a = -2, b = -1$

(B) $a = -2, b = -3$

(C) $a = -4, b = 3$

(D) $a = -4, b = -3$

(E) $a = 4, b = 3$

$g(x) = \frac{x^2 - 4}{3x^2 - 3}$

6) Identify the vertical asymptotes for $f(x) = \frac{x^2 + 3x - 4}{x^2 + x - 2}$.

(A) $x = -2, x = 1$

(B) $x = -2$

(C) $x = 1$

(D) $y = -2, y = 1$

(E) $y = -2$

$\frac{(x-1)(x+4)}{(x-1)(x+2)}$

$x = -2$