



WARM UP!!



For each of the derivatives listed below, find a possible value for $f(x)$.

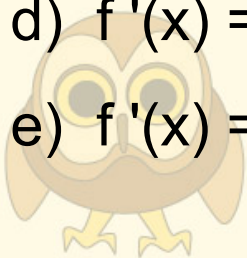
a) $f'(x) = 2x$ $f(x) = x^2 + C$

b) $f'(x) = x$ $f(x) = \frac{1}{2}x^2 + C$

c) $f'(x) = x^2$ $f(x) = \frac{1}{3}x^3 + C$

d) $f'(x) = 1/x^2$ $f(x) = -\frac{1}{x} + C$

e) $f'(x) = 1/x^3$ $f(x) = -\frac{1}{2x^2} + C$



4.1 Antiderivatives!

At the end of this lesson you will be able to:

- Understand what is meant by an antiderivative
- Write antiderivatives with proper notation
- Compute antiderivatives of simple polynomial, radical and rational functions



Antidifferentiation is the inverse operation for differentiation. (Like addition/subtraction, multiplication/division, ...)

So derivatives and antiderivatives are the results of these inverse operations (like sums/differences, products/quotients, ...)

NOTATION!!

$$\int 2x dx = x^2 + C$$

Handwritten annotations in blue ink:

- An arrow points from the integral symbol \int to the text "integral symbol".
- A bracket under $2x dx$ is labeled "integrand".
- A bracket under $x^2 + C$ is labeled "antiderivative".
- An arrow points from the text "constant of integration" to the constant C .

Integration Formulas (can you derive them?)

$$1) \int a \, dx = ax + C$$

$$2) \int x^n \, dx = \frac{1}{n+1} x^{n+1} + C$$

$$3) \int [f(x) + g(x)] \, dx = \int f(x) \, dx + \int g(x) \, dx$$

$$4) \int af(x) \, dx = a \int f(x) \, dx$$

$$5) \int f'(x) \, dx = f(x) + C$$

$$6) \frac{d}{dx} \int f(x) \, dx = f(x)$$

Let's do some together!!

$$1) \int 7x dx = 7 \cdot \frac{1}{2} x^2 + C = \frac{7}{2} x^2 + C$$

$$2) \int 7x^3 dx = \frac{7}{4} x^4 + C$$

$$3) \int [2x + 3x^2 - 5x^4] dx$$

$$= x^2 + x^3 - x^5 + C$$

Give these a try!

$$1) \int (x^3 - 4x + 2) dx = \frac{1}{4}x^4 - 2x^2 + 2x + C$$

$$2) \int \frac{4}{x^3} dx = -\frac{2}{x^2} + C$$

$$3) \int (3x - 1)^2 dx = \int (9x^2 - 6x + 1) dx = 3x^3 - 3x^2 + x + C$$

$$4) \int \frac{3x^2 - x + 1}{\sqrt{x}} dx = \int \left(3x^{\frac{3}{2}} - x^{\frac{1}{2}} + x^{-\frac{1}{2}} \right) dx$$

$$= \frac{6}{5}x^{\frac{5}{2}} - \frac{2}{3}x^{\frac{3}{2}} + 2x^{\frac{1}{2}} + C$$

$$5) \int (\theta^2 + \sin \theta) d\theta = \frac{1}{3}\theta^3 - \cos \theta + C$$

$$6) \int (1 + \cot^2 x) dx = \int \csc^2 x dx = -\cot x + C$$

$$7) \int \frac{\sin x}{\cos^2 x} dx = \int \sec x \tan x dx = \sec x + C$$

In your groups, complete each of the following antiderivative rules.

$$1) \int \sin x \, dx = -\cos x + C$$

$$2) \int \cos x \, dx = \sin x + C$$

$$3) \int \sec^2 x \, dx = \tan x + C$$

$$4) \int \sec x \tan x \, dx = \sec x + C$$

$$5) \int \csc^2 x \, dx = -\cot x + C$$

$$6) \int \csc x \cot x \, dx = -\csc x + C$$

What have we learned??

- What is an antiderivative?
- What is an indefinite integral?
- Can I antidifferentiate a basic polynomial or trigonometric function?

