

## Warmup!

1) If  $y = \sin(5x)$ , find  $y' \approx \cos(5x) \cdot 5$

$$\checkmark y' = 5\cos(5x)$$

$$y = \cos(x^2)$$

$$y' = -\sin(x^2) \cdot 2x$$

2) Suppose  $y = \sqrt{\cos(x^2)}$ , find  $dy/dx$

$$y = [\cos(x^2)]^{\frac{1}{2}}$$

$$\checkmark y' = \frac{1}{2} [\cos(x^2)]^{-\frac{1}{2}} [-\sin(x^2)] \cdot 2x$$

$$\frac{dy}{dx} = \frac{-x \sin(x^2)}{\sqrt{\cos(x^2)}}$$

## 2.4b Chain Rule with Trig!

### ESSENTIAL LEARNING TARGETS

At the end of this lesson, you will be able to:

- Apply the chain rule to differentiate composite functions

You try!

If  $f(x) = \sqrt[3]{\tan(6x^4 + 3x - 2)}$  , find  $f'(x)$

Find  $dy/dx$  for each of the following:

a)  $y = (2x + 3)^3$

m)  $y = \tan(x^2)$

b)  $y = (2x^2 + 3)^3$   $y' = 3(2x^2 + 3)^2 \cdot 4x$  n)  $y = \tan(\sin x)$

c)  $y = (2x^3 + 3)^3$  (4x) o)  $y = \cot(\sin x)$

d)  $y = \sqrt{2x + 3} = 12x(2x^2 + 3)^{1/2}$  p)  $y = \csc(\cos x)$

e)  $y = (x + 1)^3$

q)  $y = \cos^2 x$

$y' = -\csc(\cos x) \cot(\cos x) \cdot (-\sin x)$

f)  $y = (x + 1)^{-3}$

r)  $y = \cos^3 x$

g)  $y = \sin(5x)$

s)  $y = \sin^2 x$

h)  $y = \sin(x^2)$

t)  $y = \sin^9 x$

i)  $y = \sin(x^3 + 1)$

u)  $y = \sin^9(2x)$

j)  $y = \sin(\cos x)$

v)  $y = \sin^9(x^2)$

k)  $y = \sin(\tan x)$

w)  $y = \sin^9(\cos x) = [\sin(\cos x)]^9$

l)  $y = \sin(\sin x)$

$y' = 9[\sin(\cos x)]^8 \cdot \cos(\cos x) \cdot (-\sin x)$

x)  $y = \sin^{37}(\tan \pi/6) = [\sin(\tan \pi/6)]^{37}$

$y' = 0$

## Check your answers!

a)  $y' = 6(2x + 3)^2$

m)  $y' = 2x\sec^2(x^2)$

b)  $y' = 12x(2x^2 + 3)^2$

n)  $y' = \cos x \cdot \sec^2(\sin x)$

c)  $y' = 18x^2(2x^3 + 3)^2$

o)  $y' = -\cos x \cdot \csc^2(\sin(x))$

d)  $y' = 1/\sqrt{2x + 3}$

p)  $y' = \sin x \cdot \csc(\cos x) \cdot \cot(\cos x)$

e)  $y' = 3(x + 1)^2$

q)  $y' = -2\cos x \sin x$

f)  $y' = -3(x + 1)^{-4}$

r)  $y' = -3\cos^2 x \sin x$

g)  $y' = 5\cos(5x)$

s)  $y' = 2\sin x \cos x$

h)  $y' = 2x\cos(x^2)$

t)  $y' = 9\sin^8 x \cos x$

i)  $y' = 3x^2\cos(x^3 + 1)$

u)  $y' = 18\sin^8(2x)\cos(2x)$

j)  $y' = -\sin x \cdot \cos(\cos x)$

v)  $y' = 18x\sin^8(x^2)\cos(x^2)$

k)  $y' = \sec^2 x \cdot \cos(\tan x)$

w)  $y' = -9\sin^8(\cos x) \cdot \sin x$

l)  $y' = \cos x \cdot \cos(\sin x)$

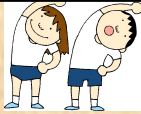
x)  $y' = 0$

## 2007 Form B #3

The wind chill is the temperature, in degrees Fahrenheit ( $^{\circ}\text{F}$ ), a human feels based on the air temperature, in degrees Fahrenheit, and the wind velocity  $v$ , in miles per hour (mph). If the air temperature is  $32^{\circ}\text{F}$ , then the wind chill is given by  $W(v) = 55.6 - 22.1v^{0.16}$  and is valid for  $5 \leq v \leq 60$ .

- (a) Find  $W'(20)$ . Using correct units, explain the meaning of  $W'(20)$  in terms of the wind chill.
- (b) Find the average rate of change of  $W$  over the interval  $5 \leq v \leq 60$ . Find the value of  $v$  at which the instantaneous rate of change of  $W$  is equal to the average rate of change of  $W$  over the interval  $5 \leq v \leq 60$ .





## Review!!



1) Find  $\frac{d(\sec(\tan x^3))}{dx}$

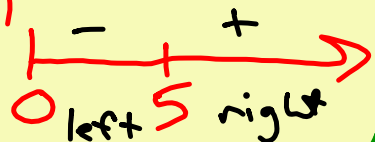
2) Given  $y = ax^2 + bx + c$  passes through  $(-2, 8)$  and is tangent to the line  $9x + y = 8$  at the point  $(1, -1)$ , find  $a$ ,  $b$  and  $c$ .

Position:  $x(t) = t^2 - 10t + 3, t \geq 0$

Velocity:  $v(t) = 2t - 10$

At rest?  $2t - 10 = 0$   
 $t = 5$  sec b/c  $v(5) = 0$

Chg direction?  $v(t)$



chgs dir @  $t = 5$  b/c  $v(t)$  chgs sign

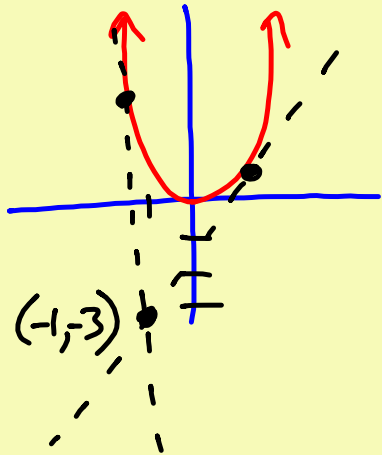
Moving left?  $(0, 5)$  b/c  $v(t) < 0$

" right?  $(5, \infty)$  b/c  $v(t) > 0$

Speed @  $t = 2$ ?  $v(2) = -6$  so speed =  $6 \frac{\text{ft}}{\text{sec}}$

Acceleration function?  $a(t) = v'(t) = 2$





$$f(x) = x^2 \quad f'(x) = 2x$$

$$y + 3 = \underline{2x} (x + 1)$$

$$y = 2x(x + 1) - 3 = x^2$$

## What have we learned?

- Can I apply the chain rule in a variety of problems and situations involving polynomial, radical, rational and trigonometric functions?

